Foundation of Intelligent Systems

Part I: Statistical Machine Learning

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Answer a Few Questions

- What is this course about?

- What kind of tools will we use?

- Do we have to program?

- For starters... a first assignment

- Why is this useful for me?

What is this course about?

Doing Science & Engineering
Using Computers $+$ Large databases

What is this course about?

- Science/engineering in 19th century

- Science/engineering in the 21st century

Goal: Use **Fast Computers** to detect and exploit patterns in **Large databases**

A typical Machine Learning Task

This course is about adaptive machines that can learn

Before...

DATA $\Rightarrow$ **Expert** (Doctor) $\Rightarrow$ **Rule**-based **hard-coded** **not reusable** program

```
if age>36 then
  if cholesterol>105mg/L then
     ...
   else
     ...
```

... now, with machine learning

DATA $\Rightarrow$ (**Meta-expert** (you!)$\rightarrow$Algorithm) $\Rightarrow$ **Adaptive** Program

What kind of mathematical tools?

We will adopt a **mathematical formalism** to propose and study algorithms.

Probability & Statistics, Linear Algebra, Optimization

Mathematical Tools

- **Probability & Statistics** *(to handle uncertainty & randomness)*

  - Probability Spaces, Random variables
  - Expectation, variance, inequalities
  - Central limit theorem, convergence in probability

- **Linear Algebra** *(to handle high-dimensional problems)*

  - Matrix inverse, eigenvalues/vectors
  - Positive-definiteness.

- **Optimization** *(to give the best possible answer)*

  - convex programs,
  - lagrangean, Lagrange multipliers *etc.*

Programming

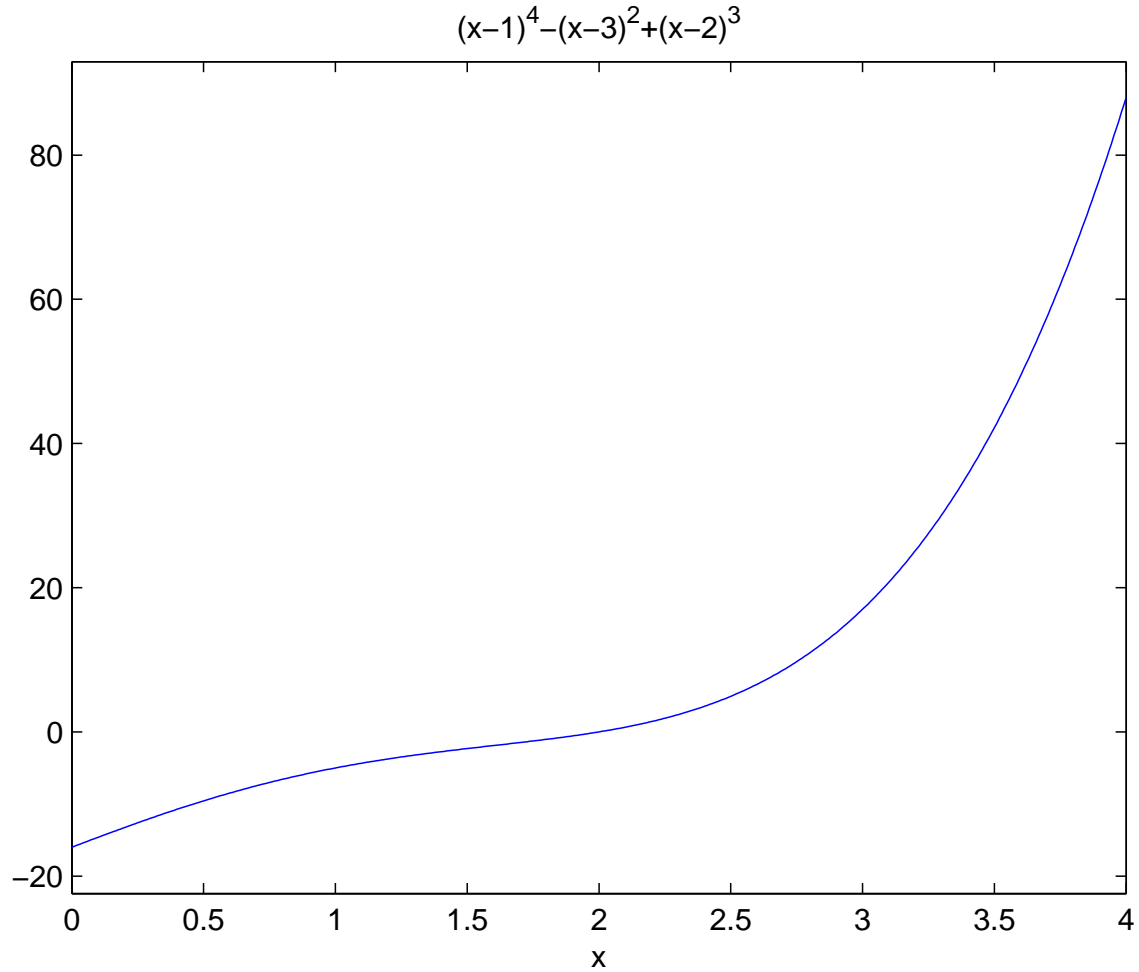This is not a course about programming, but we **will** implement algorithms

I encourage you to use **MATLAB**
but you can use any other program (R, Python, etc...)

I **do not recommend** using C/C++ or other compiled languages.

For Starters...
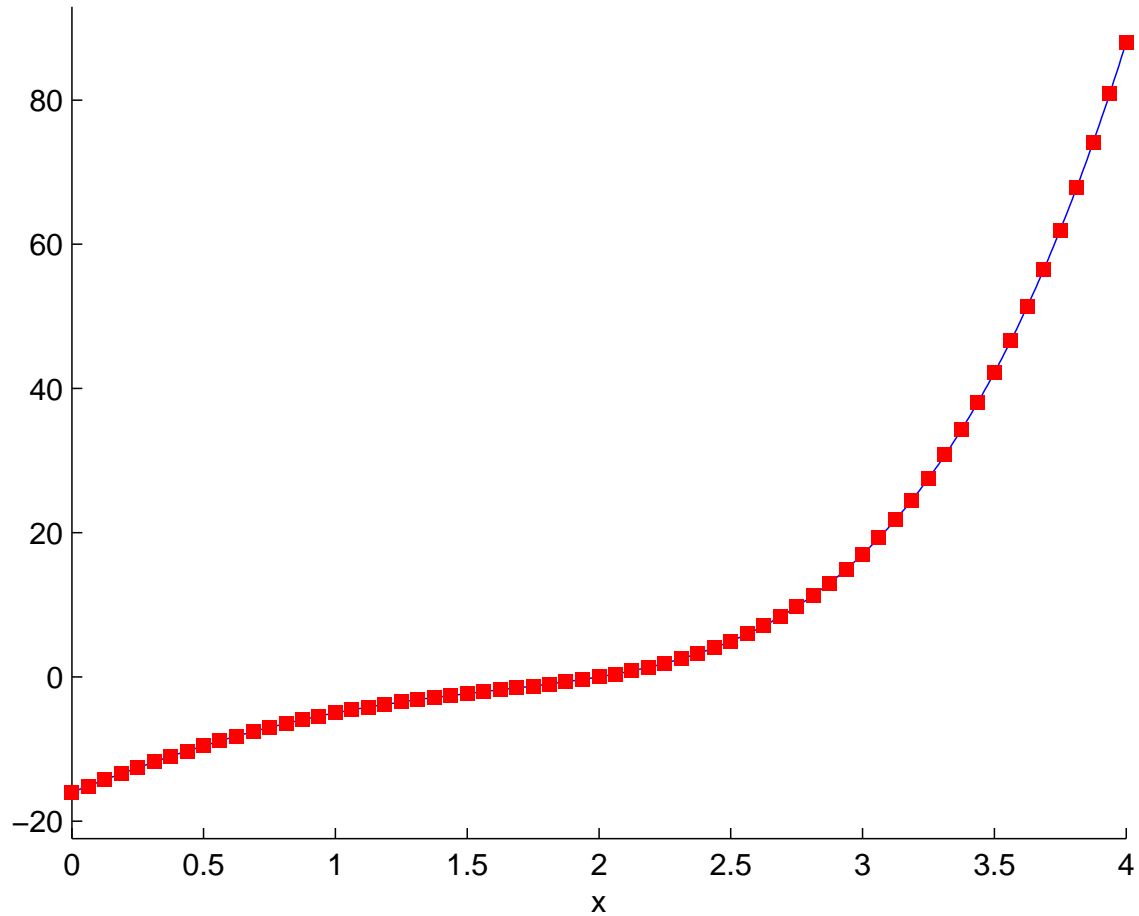
Some simple ideas and a 1st assignment.

A function

$(x-1)^4-(x-3)^2+(x-2)^3$
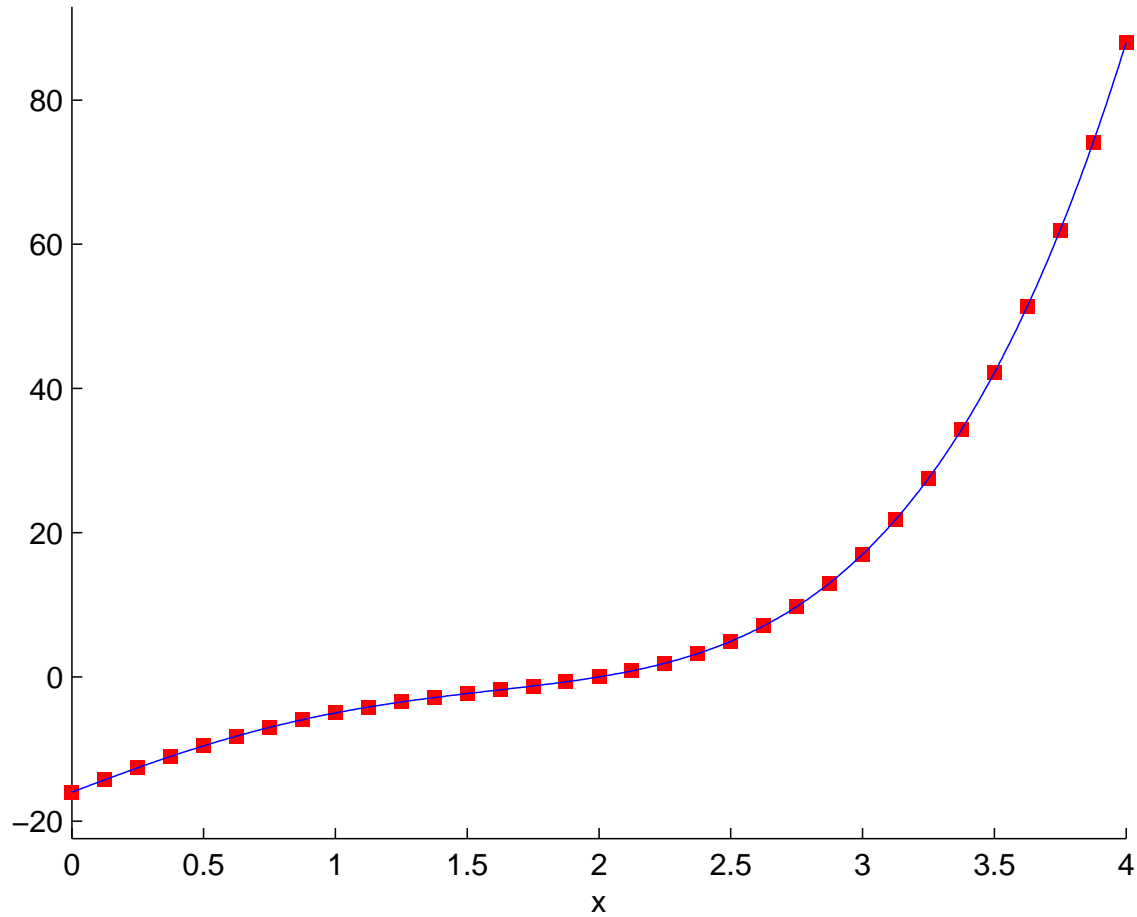
a polynomial plotted between 0 and 4...

A function

$(x-1)^4-(x-3)^2+(x-2)^3$

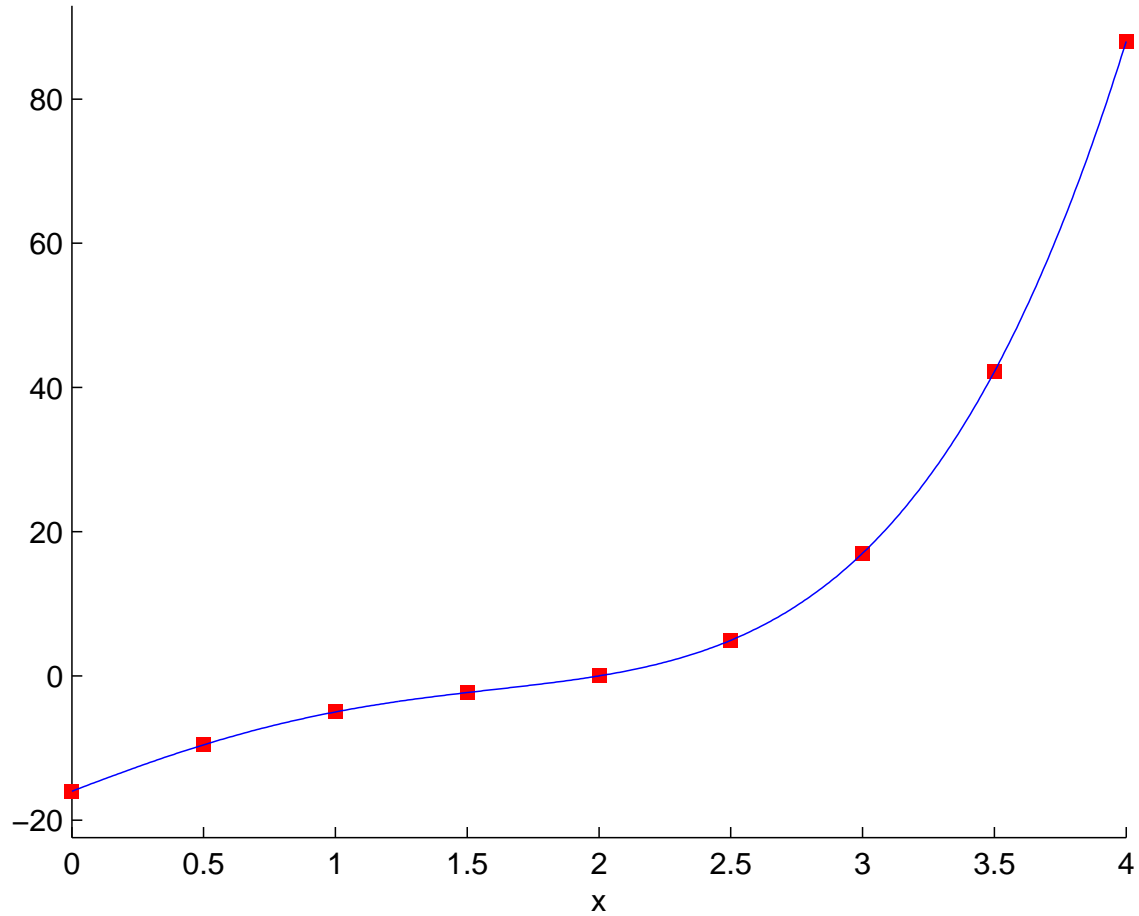... can be seen as a very detailed scatter plot.

A function

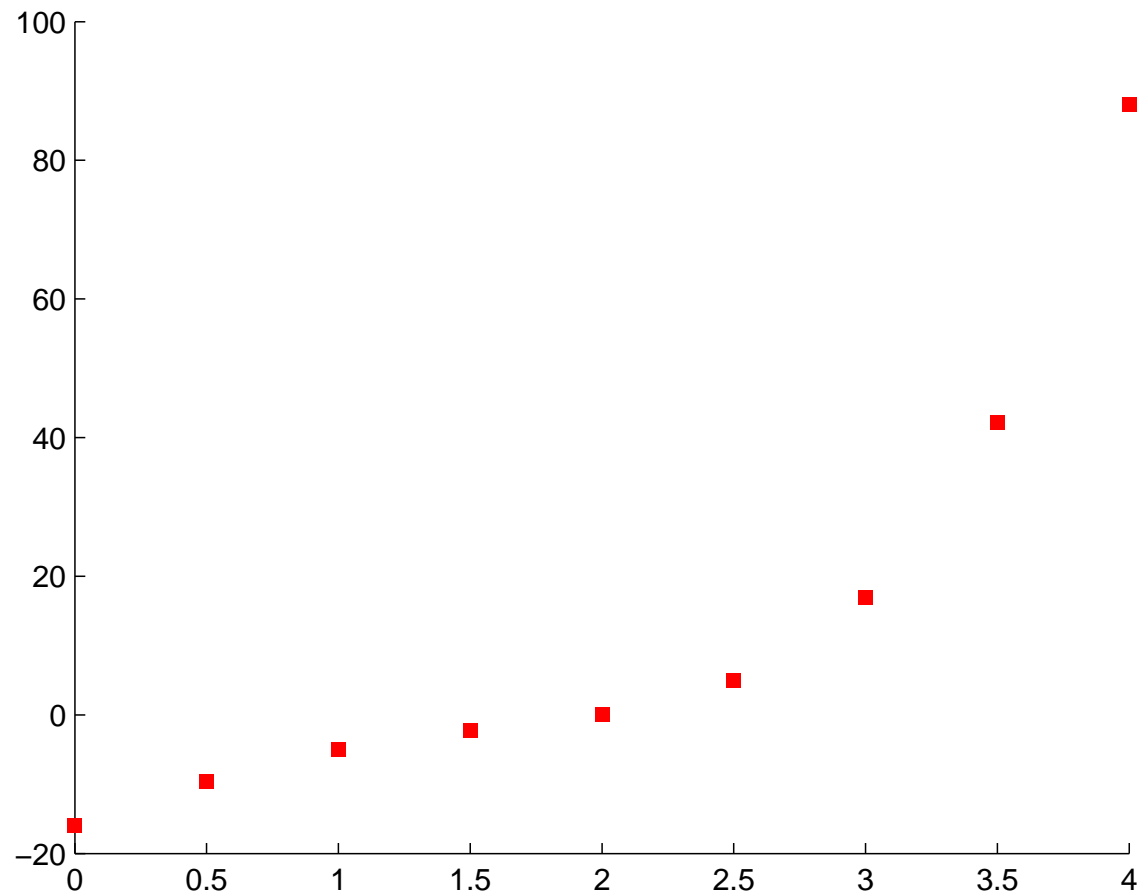$$(x-1)^4 - (x-3)^2 + (x-2)^3$$

Yet, when less points are available...
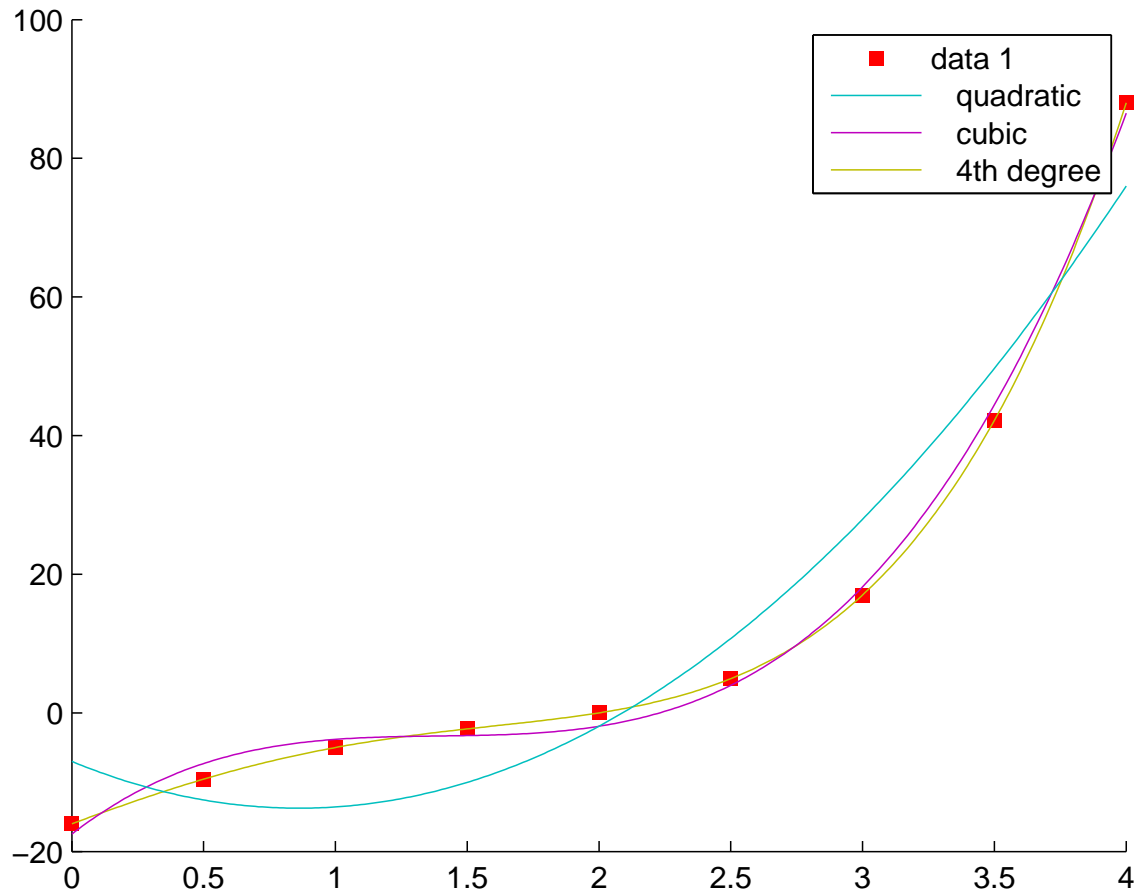
A function

$$(x-1)^4-(x-3)^2+(x-2)^3$$

can we still guess the whole blue line?
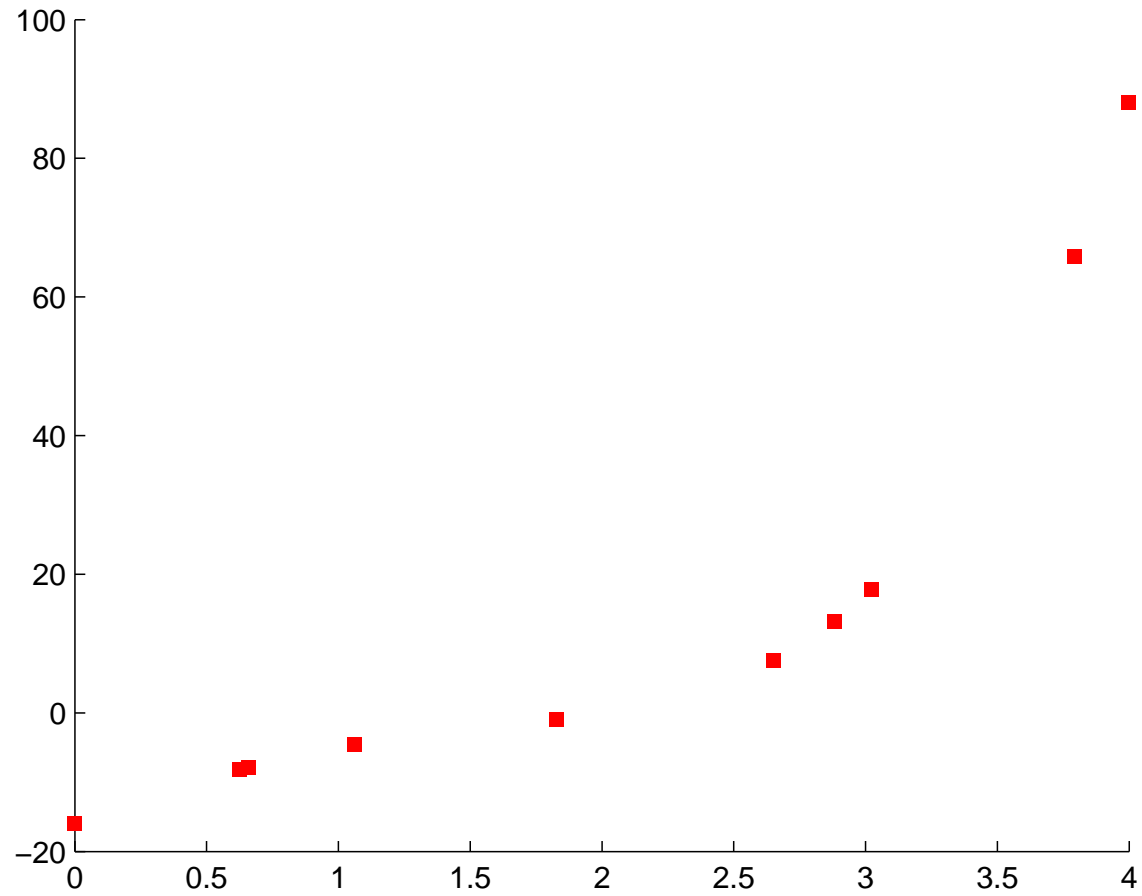
A partially observed function

Assume we only have the red points.

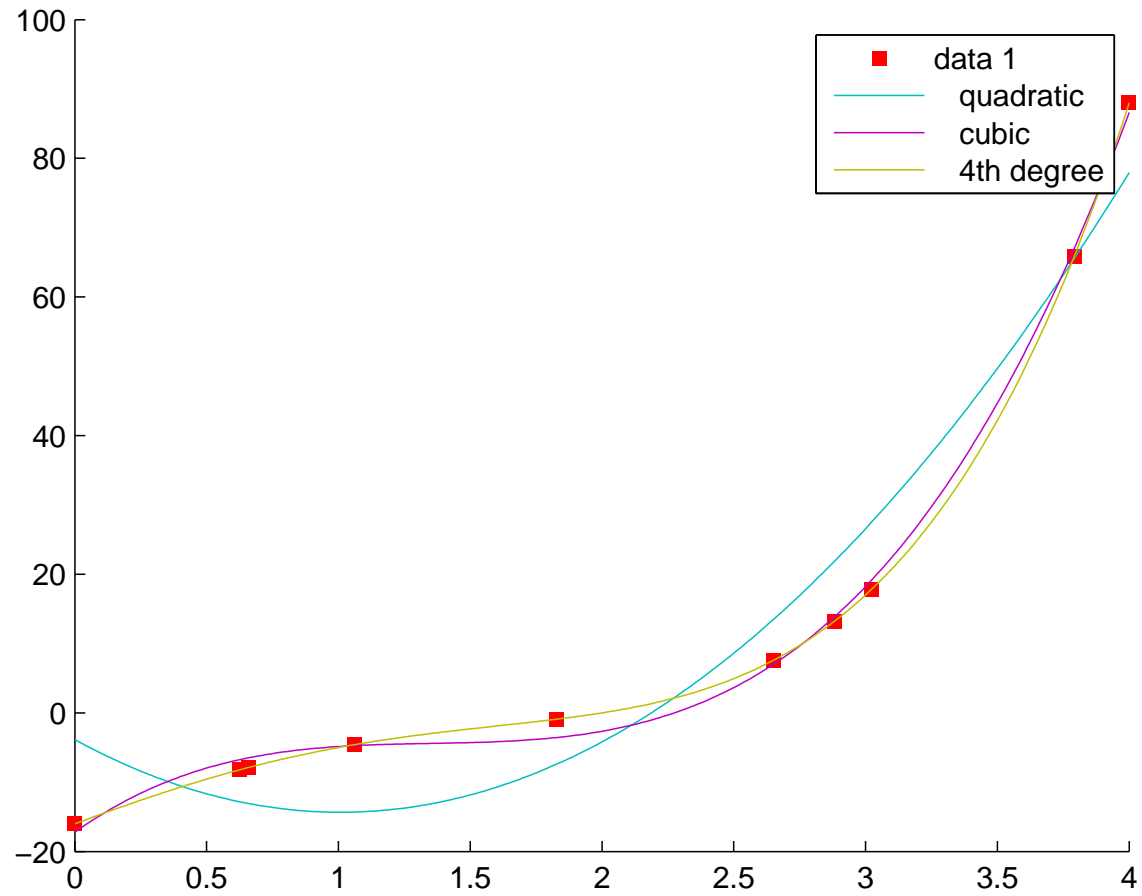# We can guess by using interpolating polynomials

Curve fitting tools can help us get back the original function.
We can actually reconstruct it **perfectly**.

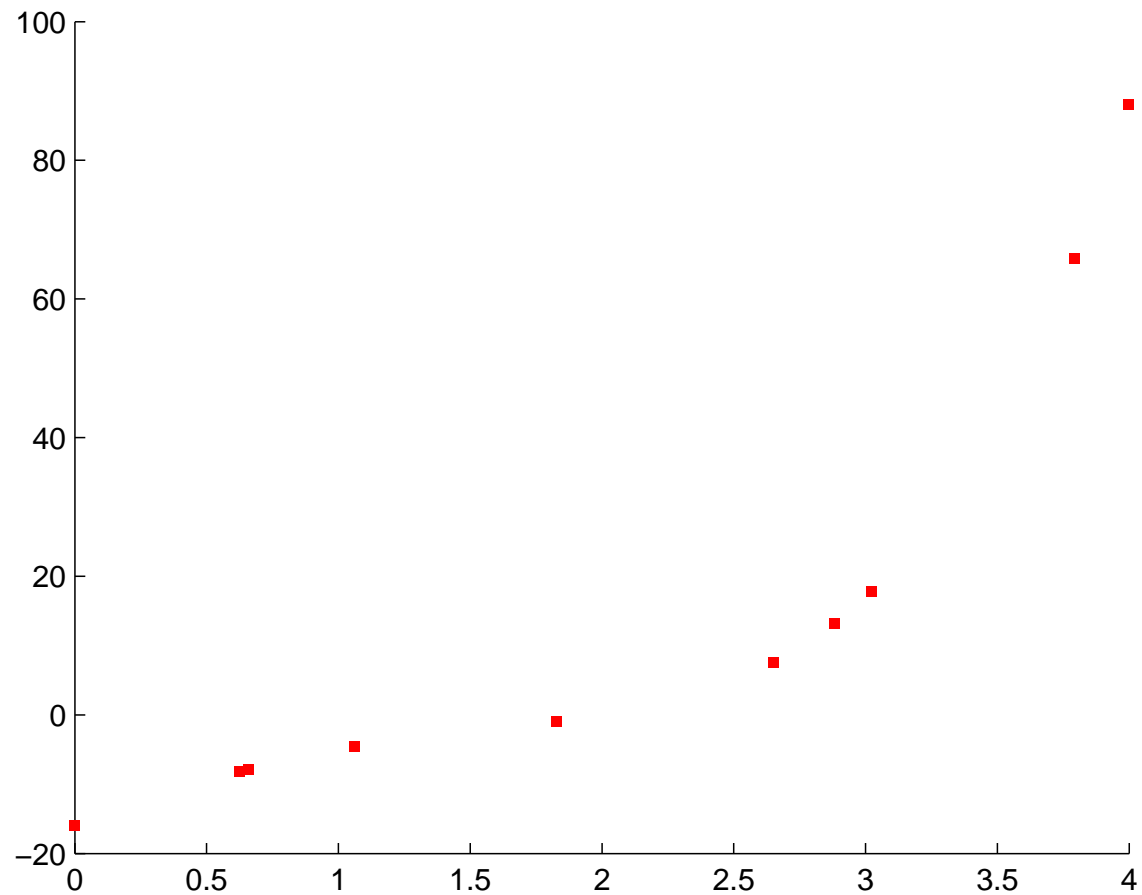# Polynomial Interpolation

even if points are not evenly spaced...
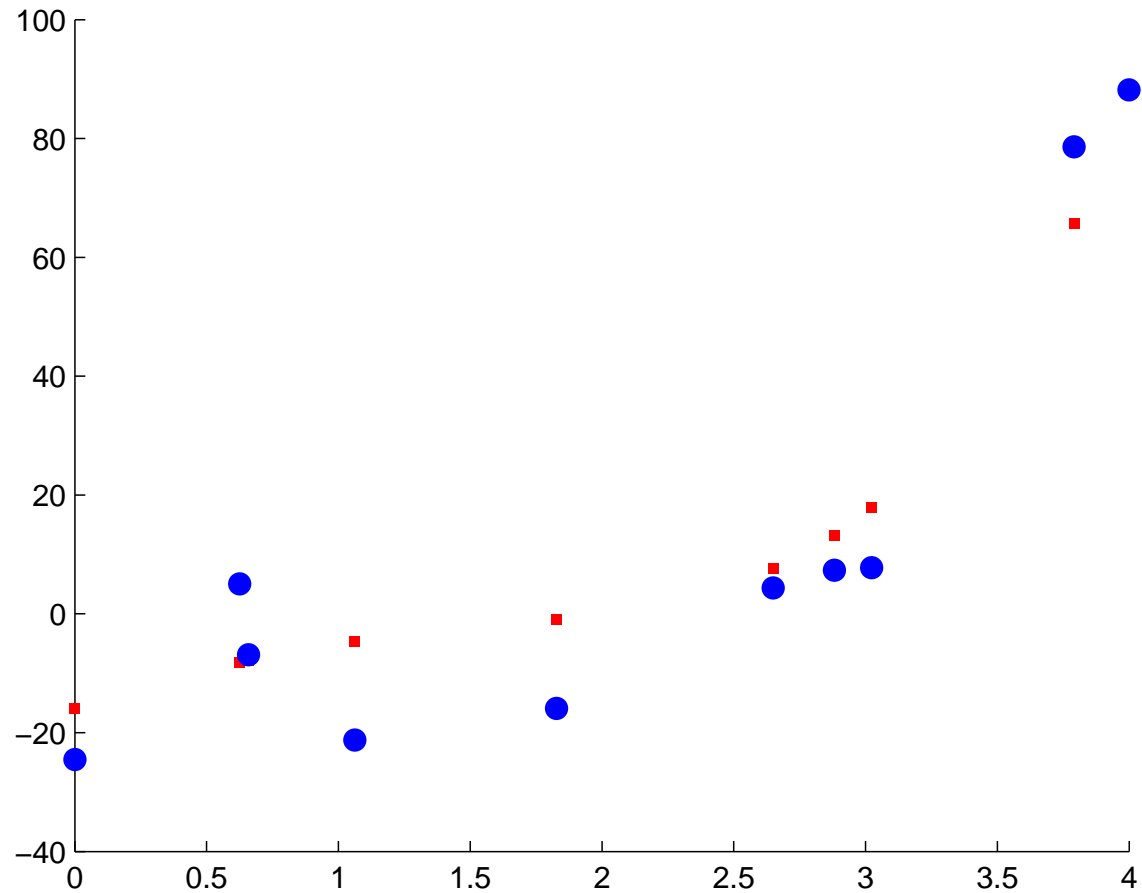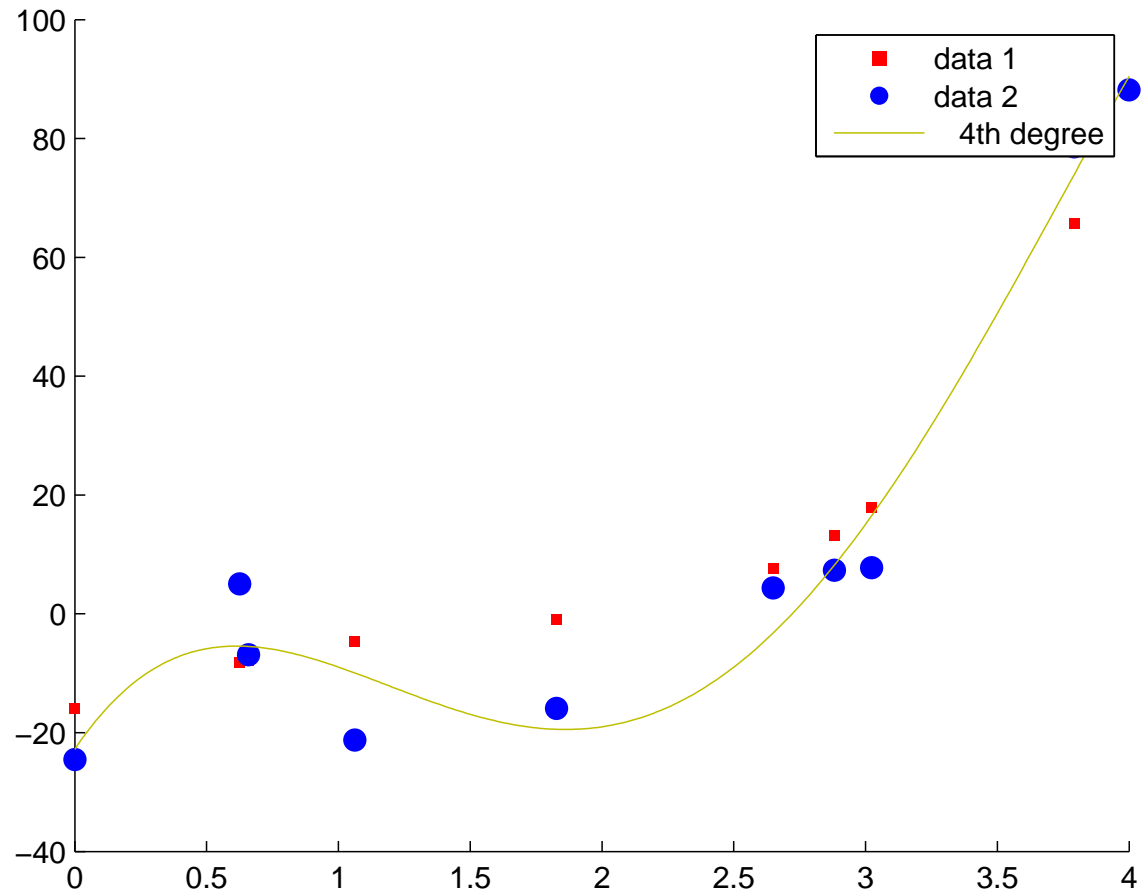
Polynomial Interpolation

Uncertainty in measurements

sometimes, we do not have access to the correct information...

Uncertainty in measurements
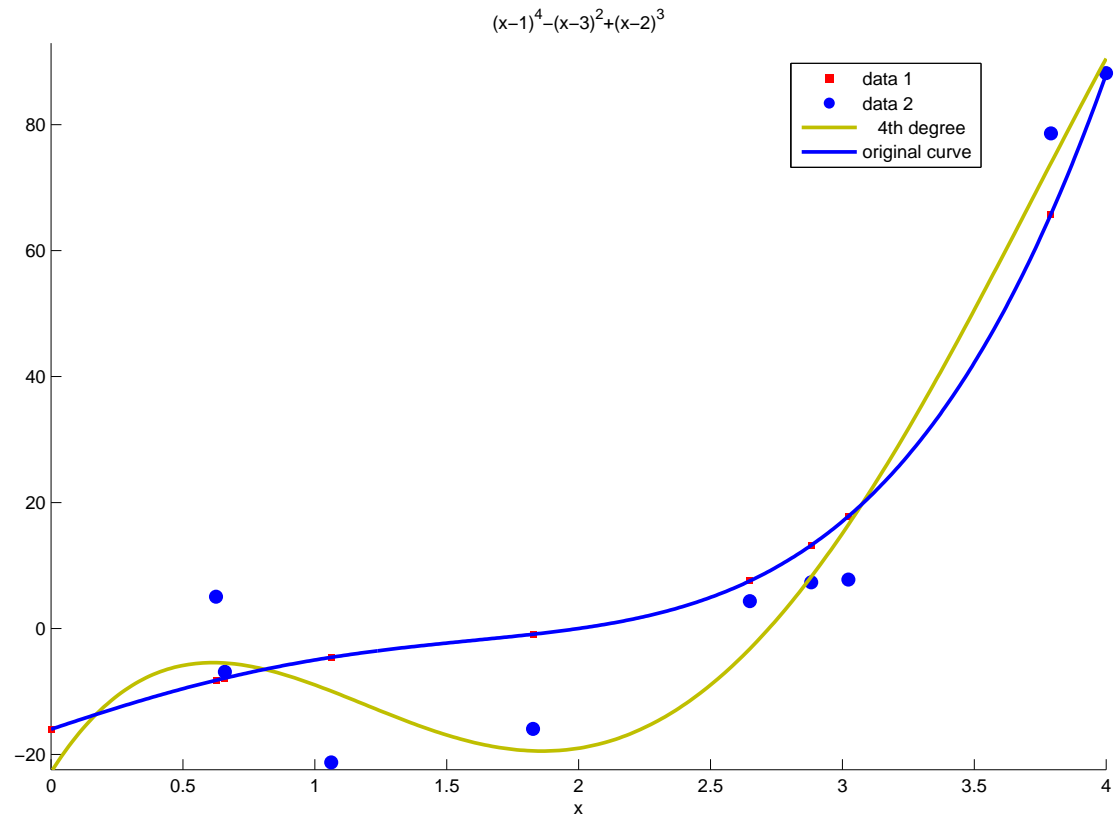

but rather an information **corrupted** by "noise".

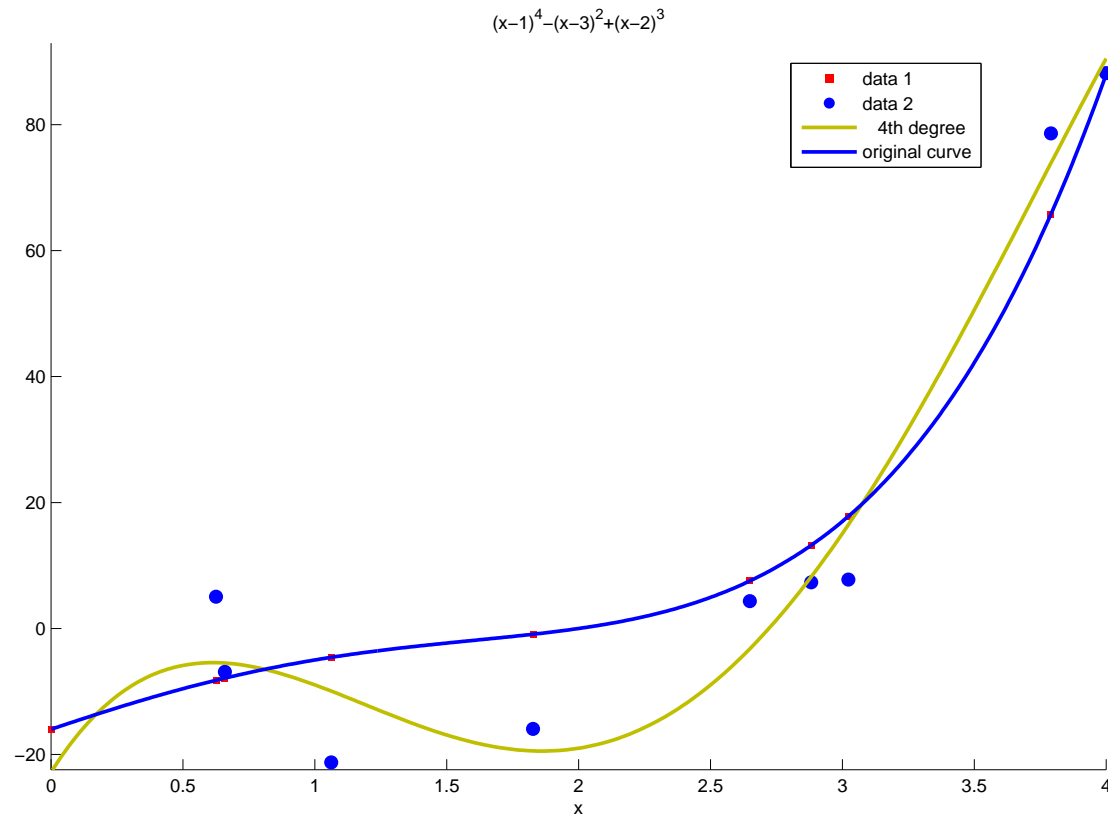# Things become a lot more difficult

If we use standard tools...

Things become a lot more difficult

we might be very far from the original function.
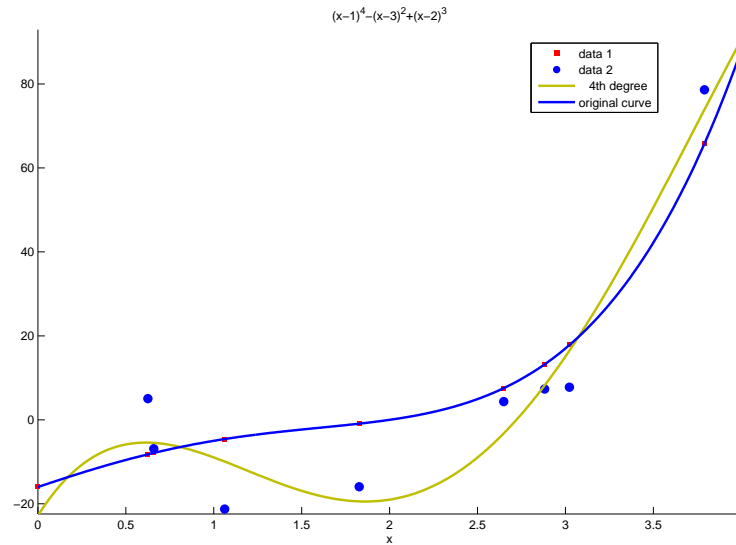
Things become a lot more difficult

Can we handle **uncertainty** in a better way?
Quantify **how far** we might be from the true function?
How many points do we need to reconstruct a more **general** curve?
Does this work for surfaces in **higher dimensions**?

Things become a lot more difficult

First assignment - due Monday 18th 23:59

- Look for a definition of interpolation, $e.g.$ check the wikipedia page.

- Do what I just did with Matlab and send me **an email** with the results:

  - Choose a function.. you can use fancier functions ($\sin, \cos, \exp$ $etc.$)
  - Plot it. Scatter plot a few points.
  - Use these points with the curve fitting tool. Interpolate & Compare.

- Finally: give me a hint of what might go wrong in higher dimensions?

To close this introduction...

Machine Learning will help you!

Taken from Computer World in 2007

...and the winner is

(See also **"The top 10 dead (or dying) computer skills"**.)

1) Machine learning

As companies work to build software such as collaborative filtering, spam filtering and fraud-detection applications that seek patterns in jumbo-size data sets, some observers are seeing a rapid increase in the need for people with machine-learning knowledge, or the ability to design and develop algorithms and techniques to improve computers' performance, Scott says.

"It's not just the case for Google," he says. "There are lots of applications that have big, big, big data sizes, which creates a fundamental problem of how you organize the data and present it to users."

Demand for these applications is expanding the need for data mining, statistical modeling and data structure skills, among others, Scott says. "You can't just wave your hand at some of these problems -- there are subtle differences in how the data structures or algorithms you choose impacts whether you get a reasonable solution or not," he explains.